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# CAS Practical Machine Learning Introduction

## Unsupervised Learning

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# Unsupervised Learning

an algorithm learns from experience  $\mathcal{E}$  to solve some tasks  $\mathcal{T}$  with performance  $\mathcal{P}$  if  $\mathcal{P}$  improves with  $\mathcal{E}$

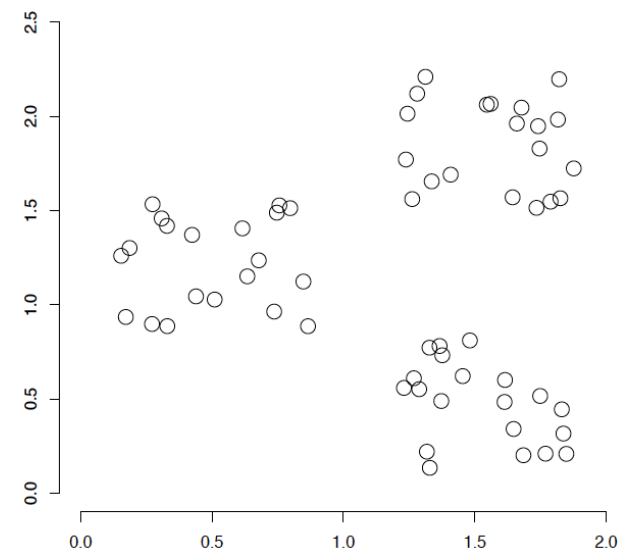
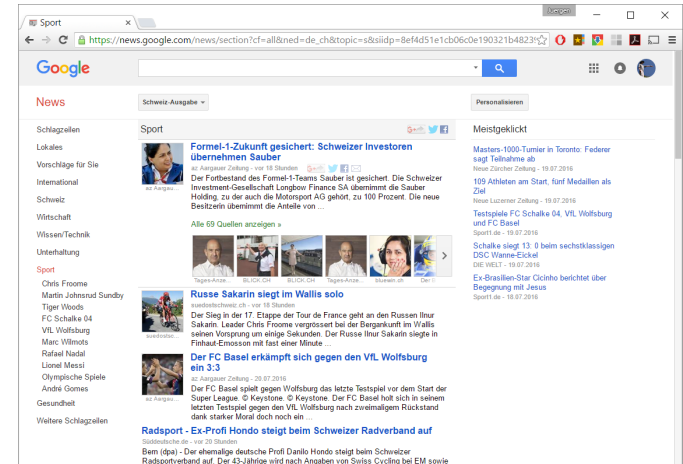
## Unsupervised Learning

- ▶ tasks  $\mathcal{T}$  that are solved
  - ▶ identifying similar items
    - ▶ e.g., recommender systems
    - ▶ e.g., collaborative filtering
  - ▶ identifying correlated features
    - ▶ e.g., dimensionality reduction
    - ▶ e.g., PCA
  - ▶ mapping a sample (based on its features) to some output
    - ▶ e.g., clustering = map to a group
    - ▶ e.g., K-Means
- ▶ the model to solve  $\mathcal{T}$  is inferred from data  $\mathcal{E}$  based on some distinctive features of  $\mathcal{E}$
- ▶ the algorithm does not have access to  $\mathcal{P}$
- ▶ the algorithm learns in the sense that more data  $\mathcal{E}$  should improve  $\mathcal{P}$

# Clustering (1)

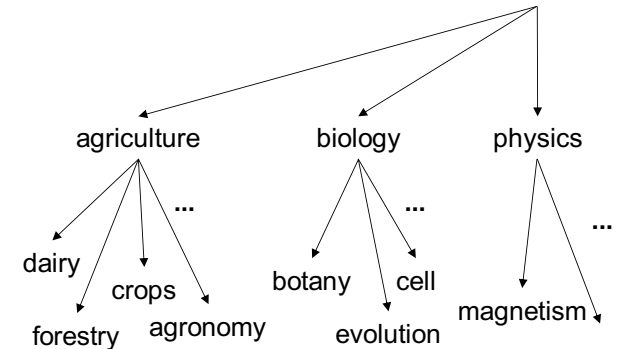
## Clustering

- ▶ aim to organize a dataset into groups, i.e., clusters
  - ▶ Iris dataset into distinct species
  - ▶ customers into target groups
  - ▶ news articles into topic groups (e.g., Google News)
  - ▶ ...
- ▶ ~ unsupervised classification
- ▶ based on some similarity measure
  - ▶ all instances within a cluster should be similar
  - ▶ and instances in different clusters should be dissimilar
- ▶ may also produce a description for each cluster discovered
  - ▶ i.e., a representative instance, a label, several labels, ....



# Clustering Documents (2)

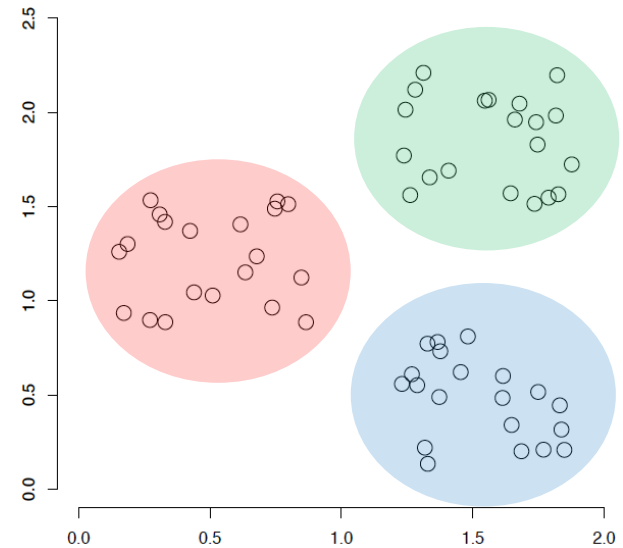
- ▶ may also build a hierarchy (relations) between clusters
- ▶ often based on unsupervised machine learning
  - ▶ i.e., can run fully automated w/o training
- ▶ may need to be fine-tuned via parameters
  - ▶ e.g., number of clusters
- ▶ tend to be computationally expensive



# Clustering via Partitioning

## Partitioning Approach

- ▶ construct a partition of  $n$  instances into a set of  $K$  clusters
  - ▶ given: a set of instance and the number  $K$
  - ▶ find: a partition of  $K$  clusters that optimizes the partitioning criterion
    - ▶ optimal?
      - ▶ intractable for many objective functions
      - ▶ in many cases would require full enumeration
    - ▶ more practical: heuristic solution



# K-Means

## Idea

- ▶ creates K clusters
- ▶ interpret samples  $x$  as real-valued vectors  $\vec{x}$ 
  - ▶ data preparation: numeric data only
- ▶ assignment of  $x$  to a cluster is based on its distance to the cluster centroids
- ▶ centroid of a cluster  $C_i$ :  $\mu(C_i) = \frac{1}{|C_i|} \sum_{\vec{x} \in C_i} \vec{x}$

## Algorithm

select K random samples  $\{c_1, c_2, \dots, c_K\}$  as approximation of centroids

until termination condition

    for each sample  $x_i$

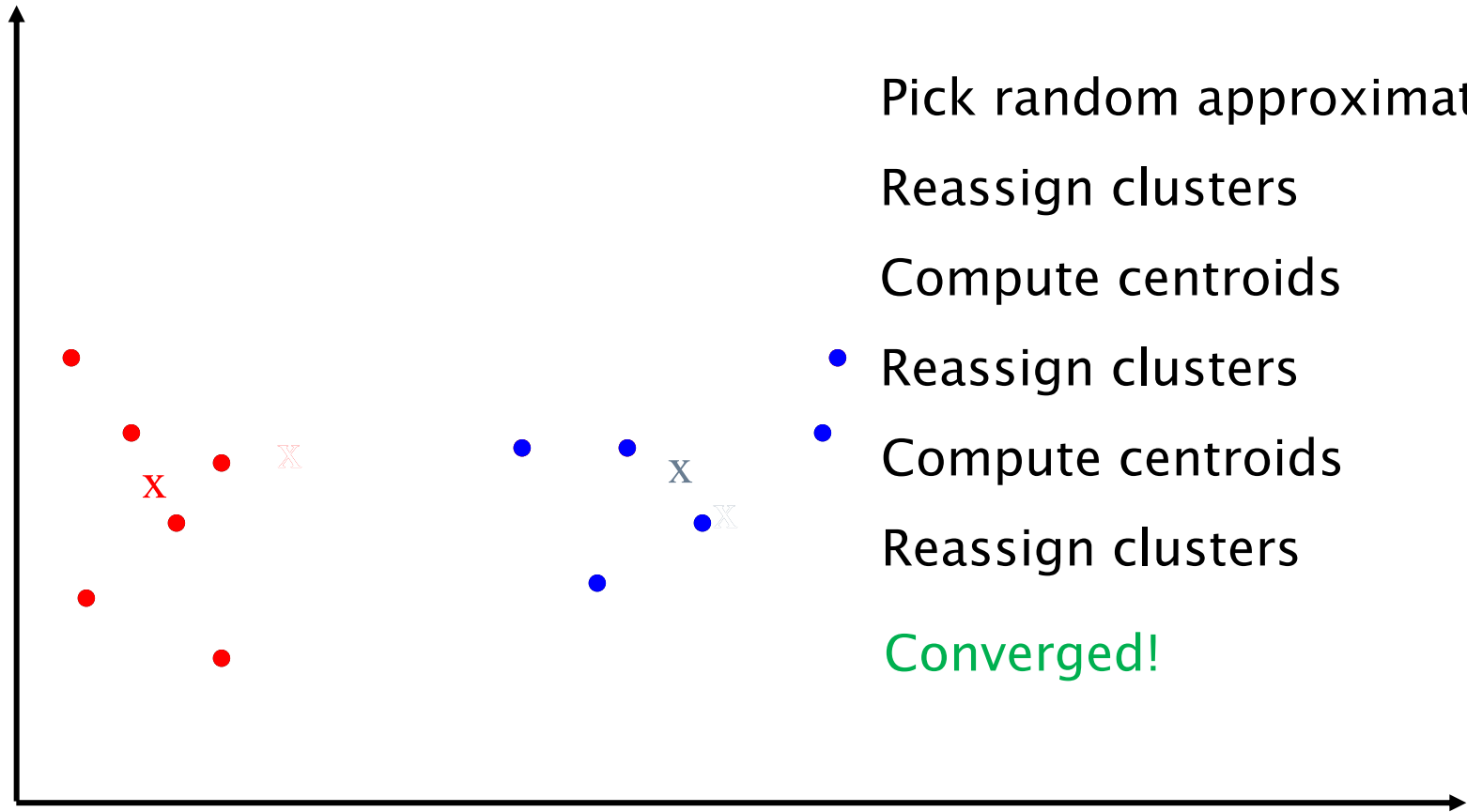
        assign  $x_i$  to the cluster  $C_j$  such that  $\text{dist}(x_i, c_j)$  is minimal

    for each cluster  $C_j$  update the approximations of centroids

$c_j = \mu(C_j)$

- ▶ termination conditions
  - ▶ clusters converge (= do not change)
  - ▶ fixed number of iterations
  - ▶ centroid positions unchanged

# K-Means Example for K=2



Pick random approximations

Reassign clusters

Compute centroids

• Reassign clusters

• Compute centroids

Reassign clusters

Converged!

# How Many Clusters $K$ ?

1. Number of clusters  $K$  is given
  - ▶ partition  $n$  samples into predetermined number of clusters
2. Finding the “right” number of clusters is part of the problem
  - ▶ partition  $n$  samples into appropriate number of clusters
  - ▶ often “try and error”
3. Use an algorithm to determine  $K$  automatically
  - ▶ define a function to assess the “quality” of all clusters
    - ▶ e.g., pairwise distance of all samples within a cluster to measure how homogenous the cluster is
  - ▶ increase  $K$  until no further quality improvement



# Discussion K-Means

## Advantages

- ▶ easy to implement and understand (“white box”)

## Disadvantages

- ▶ assumes that clusters are sphere-shaped
- ▶ number of iterations and resulting clusters results depend on seed choice
  - ▶ use heuristic rather than random picks
- ▶ algorithm may converge on local minima
  - ▶ re-run with different seeds
  - ▶ post-process resulting clusters
    - ▶ split the n “worst” clusters into 2 (or more) sub-clusters
    - ▶ merge 2 close clusters (=centroid are close) into one
- ▶ relatively slow
  - ▶ updating centroid after each new sample assignment may speed up the process

# Cluster Evaluation Metrics (1)

- ▶ in case we have a classified data set (gold standard)
  - ▶ homogeneity score
    - ▶  $\in [0; 1]$  where 1 means that each computed cluster contains only samples of one gold standard cluster
  - ▶ completeness score
    - ▶  $\in [0; 1]$  where 1 means that all samples from a gold standard cluster are assigned to the same computed cluster
  - ▶ adjusted rand index (ARI)
    - ▶ overlap between the sets of clusters (computed vs. gold standard)
      - ▶ overlap = number of common items
    - ▶  $ARI \in [-1; 1]$  where 1 means equality

# Cluster Evaluation Metrics (2)

- ▶ in case the gold standard is not known
  - ▶ sum of squared error (SSE)
    - ▶ sum of squared distance of each sample to the centroid of its assigned cluster
    - ▶ squared: penalty for samples that are far from the cluster centroid
  - ▶ silhouette coefficient
    - ▶ per sample: (normalized) average distance of sample to all other points in the same cluster – average distance of sample to all other points in the next nearest cluster
    - ▶ overall silhouette coefficient as average
    - ▶  $\in [-1; 1]$  where 1 means dense clusters